

Inference at * 2 2 1 2
of proof for Lemma p-fun-exp-add-sq:

1. $A : \text{Type}$
 2. $f : A \rightarrow (A + \text{Top})$
 3. $x : A$
 4. $m : \mathbb{Z}$
 5. $0 < m$
 6. $\forall n : \mathbb{N}. (\uparrow \text{can-apply}(f^{\wedge m - 1}; x)) \Rightarrow ((f^{\wedge n + (m - 1)}(x)) \sim (f^{\wedge n}(\text{do-apply}(f^{\wedge m - 1}; x))))$
 7. $n : \mathbb{N}$
 8. $\uparrow \text{can-apply}(f^{\wedge m}; x)$
 9. $\neg(n = 0)$
 10. $\neg(n + m = 0)$
 11. $\neg(n = 0)$
 12. $\neg(m = 0)$
- $\vdash (f \circ f^{\wedge n} (\text{do-apply}(f^{\wedge m - 1}; x))) \sim (f \circ f^{\wedge n - 1} (\text{do-apply}(f \circ f^{\wedge m - 1}; x)))$
by (RW (AddrC [2;2] (UnfoldsC “p-compose“) 0)
CollapseTHEN ((RepUR “do-apply“ (0
)·)
CollapseTHEN ((Fold ‘do-apply‘ 0)
CollapseTHEN (((if (0
) =0 then SplitOnConclITE else SplitOnHypITE (0))·)
CollapseTHENA (Auto·)·)·)
- 1:truecase. . . . NILNIL
13. $\uparrow \text{can-apply}(f^{\wedge m - 1}; x)$
 $\vdash (f \circ f^{\wedge n} (\text{do-apply}(f^{\wedge m - 1}; x))) \sim (f \circ f^{\wedge n - 1} (\text{outl}(f(\text{do-apply}(f^{\wedge m - 1}; x)))))$
- 2:falsecase. . . . NILNIL
13. $\neg(\uparrow \text{can-apply}(f^{\wedge m - 1}; x))$
 $\vdash (f \circ f^{\wedge n} (\text{do-apply}(f^{\wedge m - 1}; x))) \sim (f \circ f^{\wedge n - 1} (\text{outl}(f^{\wedge m - 1}(x))))$
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